

Valuation Fundamentals

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Summary

- Determine how financial analysts perform valuations and study the drivers of fluctuations in expected valuations
- 78,509 equity reports ensures a direct measure of short and medium-term growth expectations, terminal growth expectations and discount rates.
- Terminal growth expectations and discount rates are the main drivers of valuation, yet discount rates explain the majority of variance.
- Analysts' methods largely follow theoretical recommendations

Introduction

- Limited consensus on whether future cash flows or discount rates explain most of the fluctuation in valuation prices
- DCF data on growth expectations and discount rates is needed to identify the key drivers of expected valuations
- By decomposing expected valuations into their components, it is observed the connection between subjective expectations and objective factors like discount rates
- The valuation components are also decomposed into key elements to identify their drivers

Data overview

- The dataset consists of 78,509 DCF equity reports published by analysts covering 11,171 firms from 94 countries, collected over 24 years (2000–2023) in the first months of each year (01/01 to 01/04).
- Country-level data on inflation rates and the 10-year treasury yield from Refinitiv and real GDP growth rate from the World Bank
- Direct observation of analysts' models, not just aggregated data like in many prior studies neither have estimated or “backed out” any of the variables
- Key inputs:
 - Discount rates: equity betas, risk premia, and risk-free rates
 - Terminal growth rates: effects of GDP, inflation and long-term interest rate

Methodology – DCF is the workhorse for valuation, but is non-linear (so hard to do regression analysis)

- Set the usual forecast for 3 years + terminal growth rate.

- Original DCF:

$$E_0^*[P_0] = \frac{E_0^*[CF_1]}{(1+E_0^*[r])^1} + \frac{E_0^*[CF_2]}{(1+E_0^*[r])^2} + \frac{E_0^*[CF_3]}{(1+E_0^*[r])^3} + \sum_{i=4}^{\infty} \frac{E_0^*[CF_3] * (1+E_0^*[g_T])^{i-3}}{(1+E_0^*[r])^i}$$

- Terminal value multiple = $\frac{1}{(E_0^*[r] - E_0^*[g_T])}$

- By simplifying the model with a short-term focus and isolating the discount rate, the DCF can be expressed by:

$$E_0^*[P_0] \approx \frac{E_0^*[CF_1]}{(1+E_0^*[r])} + \frac{E_0^*[P_1]}{(1+E_0^*[r])} \Rightarrow 1 + E_0^*[r] = \frac{E_0^*[CF_1] + E_0^*[P_1]}{P_0}$$

Methodology – Linearizing DCF

- To highlight the key inputs, the DCFs are linearized by the Campbell-Shiller decomposition:

- $1 + E_0^*[r] = \frac{E_0^*[CF_1] + E_0^*[P_1]}{P_0}$

- $\ln(E_0^*[CF_1] + E_0^*[P_1]) \approx \ln(E_0^*[CF_1]) + \rho \ln\left(\frac{E_0^*[P_1]}{E_0^*[CF_1]}\right)$

- $\ln(1 + E_0^*[r]) = \ln(E_0^*[CF_1]) + \rho \ln\left(\frac{E_0^*[P_1]}{E_0^*[CF_1]}\right) - \ln(P_0)$

- $\ln(1 + E_0^*[r]) = k - \ln(E_0^*[P_0]) + \ln(CF_0) + \ln\left(\frac{E_0^*[FCF_1]}{FCF_0}\right) + \rho \ln\left(\frac{E_0^*[P_1]}{E_0^*[CF_1]}\right) \Rightarrow$

$\Rightarrow \ln(E_0^*[P_0]) = k + \ln(CF_0) - \ln(1 + E_0^*[r]) + \ln\left(\frac{E_0^*[FCF_1]}{FCF_0}\right) + \rho \ln\left(\frac{E_0^*[P_1]}{E_0^*[CF_1]}\right)$ ρ being a normalizing constant smaller than 1 and by iterating forward:

$$\ln(E_0^*[P_0]) = k + \ln(CF_0) + \ln(1 + E_0^*[g_1]) + \rho \ln(1 + E_0^*[g_2]) + \rho^2 \ln(1 + E_0^*[g_3]) + \frac{\rho^3}{1 - \rho} \ln(1 + E_0^*[g_T]) - \frac{1}{1 - \rho} \ln(1 + E_0^*[r])$$

- This allows to express DFCs as a **LINEAR function** of variables that are determined and observable at the time of the forecast: growth expectations and discount rate

Valuation – Regression

- Y: valuation i, j, t : valuation from company i , analyst j and forecast year t
- Both growth expectations and discount rate are associated with changes in analysts' expected valuation

Panel A: DCF		$\ln(\text{Valuation}_{i,j,t})$					
	All sample			Younger firms			All sample
	Free cash flows						Sales
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Terminal growth $_{i,j,t}$	10.48*** (1.74)	4.88*** (1.27)	6.90** (3.22)	9.50*** (2.71)	8.45*** (1.83)	18.83*** (6.55)	11.39** (4.84)
Discount rate $_{i,j,t}$	-20.16*** (1.35)	-13.22*** (1.06)	-16.47*** (3.51)	-13.75*** (2.00)	-14.48*** (1.70)	-19.91*** (5.39)	-19.13*** (3.95)
Initial value $_{i,j,t}$			0.06** (0.03)			0.07 (0.04)	0.09 (0.08)
Short-term growth $_{i,j,t}^{\text{Year} = 1}$			0.00 (0.05)			0.08 (0.09)	-0.02 (0.09)
Medium-term growth $_{i,j,t}^{\text{Year} = 2-3}$			0.22*** (0.08)			0.34** (0.14)	0.15 (0.12)
Contributor*Firm FE	No	Yes	Yes	No	Yes	Yes	Yes
Observations	18,578	12,058	413	5,934	3,507	143	384
F Statistics	120.83	83.55	5.75	28.09	53.11	6.39	6.74
R^2	0.04	0.93	0.92	0.02	0.94	0.94	0.92

Valuation – R² Decomposition

- Firm expected valuation

Panel A: DCF	ln(Valuation _{<i>i,j,t</i>})						
	All sample			Younger firms			All sample
	Free cash flows						Sales
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
Contributor*Firm FE	No	Yes	Yes	No	Yes	Yes	Yes
<i>R</i> ² Decomposition							
Initial value ^{Year = 0} _{<i>i,j,t</i>}			8.15 %			6.32 %	8.15 %
Discount rate (DR) _{<i>i,j,t</i>}	90.07 %	81.82 %	71.04 %	83.09 %	51.59 %	42.17 %	71.04%
Short-term growth ^{Year = 1} _{<i>i,j,t</i>}			3.32 %			10.91%	3.32 %
Medium-term growth ^{Year = 2-3} _{<i>i,j,t</i>}			6.10 %			8.66 %	6.10 %
Terminal growth (TGR) _{<i>i,j,t</i>}	9.93 %	18.18 %	11.39 %	16.91 %	48.41 %	31.94 %	11.39%

- Long-term expectations are more important than short-term to explain aggregate market prices fluctuation, but discount rates are associated with the greatest amount of variations in expected prices
- The discount rate is consistently the most explanatory factor, explaining most of the variance in expected valuations across all models.
- This makes the discount rate the single most important input to understand expected prices

Valuation – Terminal Value Multiple

- The terminal value accounts for about 70% of the total equity valuation
- Two inputs: discount rate and the terminal growth rate
- Once again the bulk of variance is explained by the discount rate, yet the effect size is similar.

$$TV M_0 = \frac{1}{r - g_T}$$

$$TV M_0 = \frac{1}{(1 + g_T)(e^{\ln(\frac{1+r}{1+g_T})} - 1)}$$

$$\ln(TV M_0) \approx -\ln(1 + g_T) - \ln(e^{\ln(\frac{1+r}{1+g_T})} - 1)$$

$$\ln(TV M_0) \approx k + (\theta - 1) * \ln(1 + g_T) - \theta \ln(1 + r)$$

Panel B: Terminal Multiple	$\ln(1/(DR_{i,j,t} - TGR_{i,j,t}))$	
	(1)	(2)
Terminal growth $_{i,j,t}$	10.48*** (1.38)	14.01*** (0.92)
Discount rate $_{i,j,t}$	-15.37*** (0.21)	-16.38*** (0.18)
Contributor*Firm FE	No	Yes
Observations	48,857	37,617
F Statistics	15,641.63	4,868.67
R ²	0.81	0.95
R ² Decomposition		
Discount rate $_{i,j,t}$ (%)	72.79 %	59.47 %
Terminal growth rate $_{i,j,t}$ (%)	27.21 %	40.53 %

Curiosity not directly relevant for the analysis of valuation drivers:

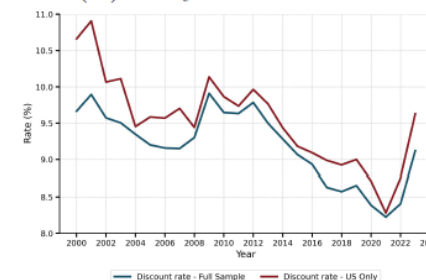
Higher terminal growth rates are associated with lower realized returns.

Dependent variable	Realized return _{t,t+1}		
	(1)	(2)	(3)
Terminal growth rate _{t,j,t}	-0.80*** (0.29)		-1.12*** (0.31)
Discount rate _{t,j,t}		0.62*** (0.16)	0.85*** (0.22)
Constant	5.58*** (0.72)	-0.96 (1.40)	-1.36 (1.85)
Observations	16,717	26,726	16,024
F Statistics	7.39	14.59	11.89
R ²	0.00	0.00	0.00

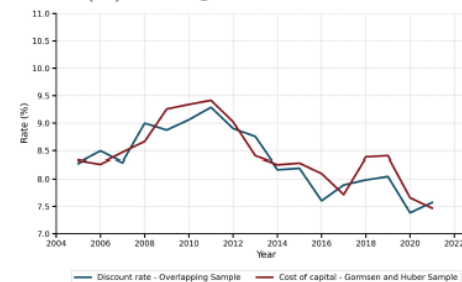
Discount Rates – Descriptive Analysis

- Benchmark
- The discount rates used by the analysts are consistent with the secular decline in the risk-free rate
- Analysts discount rates, on average, track the discount rates used by the management.
- Their similarities suggest that firm managers and equity analysts measure the cost of capital with comparable methods

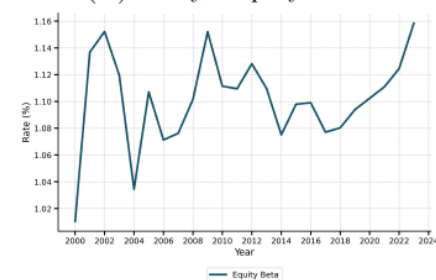
(A) Analyst discount rates.



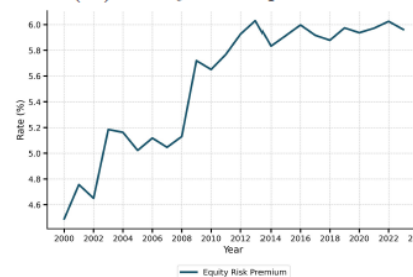
(B) Managers discount rates.



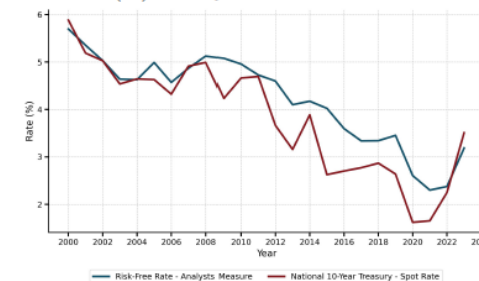
(C) Analyst equity betas.



(D) Analyst risk premium.

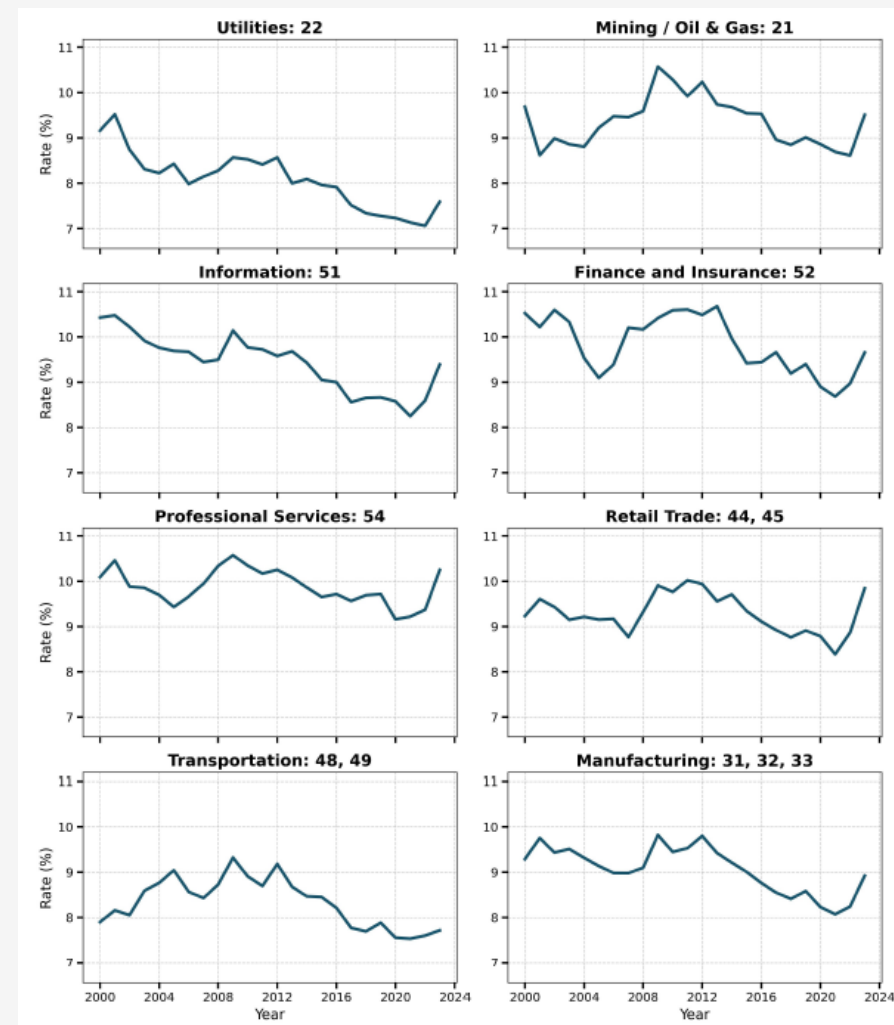


(E) Analyst risk-free rate.



Discount Rate – Descriptive Analysis

- There are systematic differences on discount rates of different industries yet follow roughly similar trends.
- Utilities, tech, manufacturing and transportation saw some decline on discount rates.
- Comdty, retail, professional services and manufacturing did not.



Discount Rates – Key Determinants Regression

- Key determinants: risk-free rates, equity beta and equity premium

Panel A: Discount rate	Discount rate _{i,j,t} (%)					
	(1)	(2)	(3)	(4)	(5)	(6)
Discount rate _{i,j,t} (%)	0.73*** (0.01)					
Analysts' risk-free rate _{i,j,t} (%)		0.46*** (0.01)			0.58*** (0.02)	0.48*** (0.03)
Analysts' equity beta _{i,j,t} (%)			2.56*** (0.07)		3.12*** (0.08)	2.52*** (0.14)
Analysts' equity risk premium _{i,j,t} (%)				0.18*** (0.02)	0.41*** (0.02)	0.35*** (0.03)
Contributor*Firm FE	No	No	No	No	No	Yes
Observations	32,798	18,466	20,966	18,868	13,328	8,789
F Statistics	3,930.60	1,238.49	1,171.29	132.75	787.38	190.76
R ²	0.52	0.15	0.13	0.02	0.39	0.82

- All three key determinants are significant, both together and individually
- The discount rate's autocorrelation (0.73) is less than the 10-year Treasury yield's (0.86), indicating that analysts' discount rates change more frequently than the risk-free benchmark

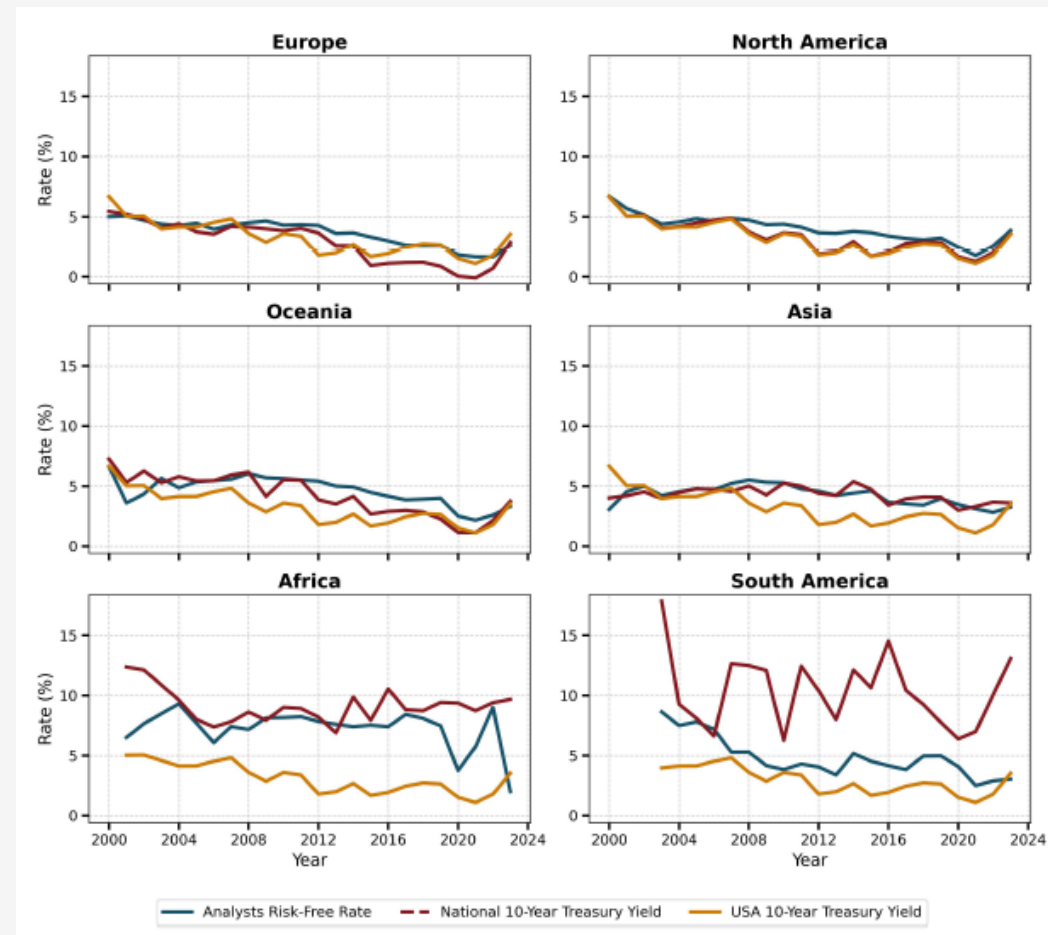
Discount Rates – Key Determinants R^2 decomposition

Panel A: Discount rate	Discount rate _{i, j, t} (%)	
	(5)	(6)
Contibutor*Firm FE	No	Yes
R^2 Shapley Decomposition		
Analysts' risk-free rate _{i, j, t} (%)	47.86 %	45.74 %
Analysts' equity beta _{i, j, t} (%)	40.55 %	42.37 %
Analysts' equity risk premium _{i, j, t} (%)	11.58 %	11.89 %

- Risk-free and equity beta consistently explain a significant portion of the discount rate variance,
- Systematic risk (risk-free and beta) explains 4x more of the discount rate process than the equity risk premium.
- To understand better each key determinant, they are analyzed one by one

Risk-free Rate – Descriptive

- Analysts' risk-free rate and the treasury yield follow the same pattern over the sample.
- Risk-free rates change over regions, making the local-specific 10-year treasury yield better to track the risk-free.



Risk-free Rate – Regression

- Also considering the monthly standard deviation of the 10-year Treasury yield during the previous year, the analysis on how analysts create their risk-free rate is shown below:

Panel B: Risk-Free Rate Volatility	Analysts' risk-free rate $_{i,j,t}$ (%)		
	(1) Full Sample	(2) 10-Year Only	(3) US Only
Analysts' risk-free rate $_{i,j,t-1}$ (%)	0.66*** (0.02)	0.70*** (0.05)	0.69*** (0.03)
10-year treasury yield $_{i,j,t}$ (%)	0.21*** (0.02)	0.29*** (0.06)	0.50*** (0.06)
10-year treasury yield $_{i,j,t}$ *Volatility $_{i,j,t-1}^{RF}$ (%)	-0.01*** (0.00)	-0.08** (0.03)	-0.22*** (0.04)
Volatility $_{i,j,t-1}^{RF}$	0.13*** (0.02)	0.56*** (0.18)	0.57*** (0.12)
Observations	6,051	607	1,407
F Statistics	1782.00	186.29	480.98
R^2	0.71	0.72	0.64

- As the 10-year treasury yield coefficient is consistently lower than the previous analyst risk-free rate, changes in 10-year treasury yield are not directly reflected in the choice of the risk-free rate
- The volatility interaction means that volatile times are associated with a reduction in the weight analysts put on the 10-year Treasury yield

Risk-free Rate – Regression

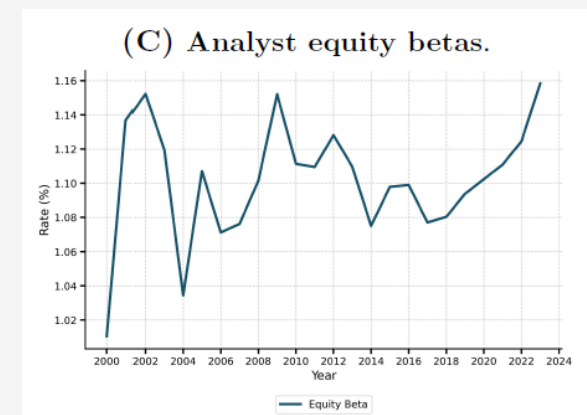
- Just like with discount rates, expectations also explain more the risk-free rates rather than current and historical average inflation

Panel D: Risk-free rate and Inflation	Analysts' risk-free rate _{c,t} (%)			US 10-year treasury yield _{c,t} (%)
	(1)	(2)	(3)	(4)
Inflation _{c,t} (%)	-0.00*** (0.00)			
10-year hist. avg. inflation _{c,t} (%)		-0.00*** (0.00)		
SPF 10-year forecast inflation _{c,t} (%)			5.19*** (1.69)	7.59*** (1.65)
Country FE	Yes	Yes	No	No
Observations	1,053	1,013	24	24
F Statistics	463.49	136.14	9.42	21.11
R ²	0.00	0.00	0.42	0.52

- By and large, the choice of risk-free rate is based on the region the analyst is in, expectations are their drivers and analysts filter out the noise so that the risk-free rate is more persistent in periods of high volatility

Equity Betas – Descriptive

- Average daily beta suggests the firms face a reasonable range of exposure to systematic risk
- To illustrate the choice of betas, the analysts' beta value is regressed on 6 different CAPM betas calculated with monthly returns for 2, 3, 4, 5, 6 and 7-years horizon.
- The 5-year one is the one that mostly explain the variance, **showing that analysts prefer to use 5-year betas**

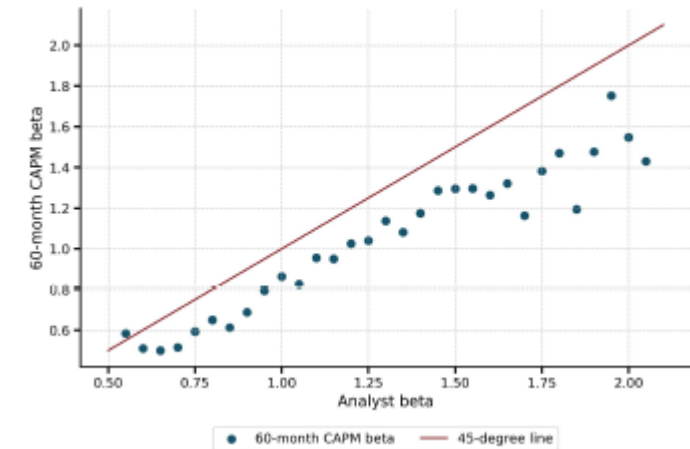


Panel A: Decomposition	Analyst beta _{i,j,t} (1)
24-month CAPM beta _{i,j,t}	-0.01** (0.01)
36-month CAPM beta _{i,j,t}	0.04*** (0.01)
48-month CAPM beta _{i,j,t}	0.04*** (0.01)
60-month CAPM beta _{i,j,t}	0.11*** (0.01)
72-month CAPM beta _{i,j,t}	0.02*** (0.01)
Observations	15,934
F Statistics	607.50
R ²	0.16
R ² Shapley Decomposition	
24-month CAPM beta _{i,j,t}	11.79%
36-month CAPM beta _{i,j,t}	19.37%
48-month CAPM beta _{i,j,t}	23.68%
60-month CAPM beta _{i,j,t}	27.59%
72-month CAPM beta _{i,j,t}	17.57%

Equity Betas – Regression

- **Analysts track the CAPM betas well**, but the relation is weaker with larger values of betas
- However, when the 1-year realized returns are regressed on analysts' betas and CAPM betas, the noise is not as prevalent showing a sharper and steeper relation:

(A) Analyst betas versus CAPM 60-month betas.



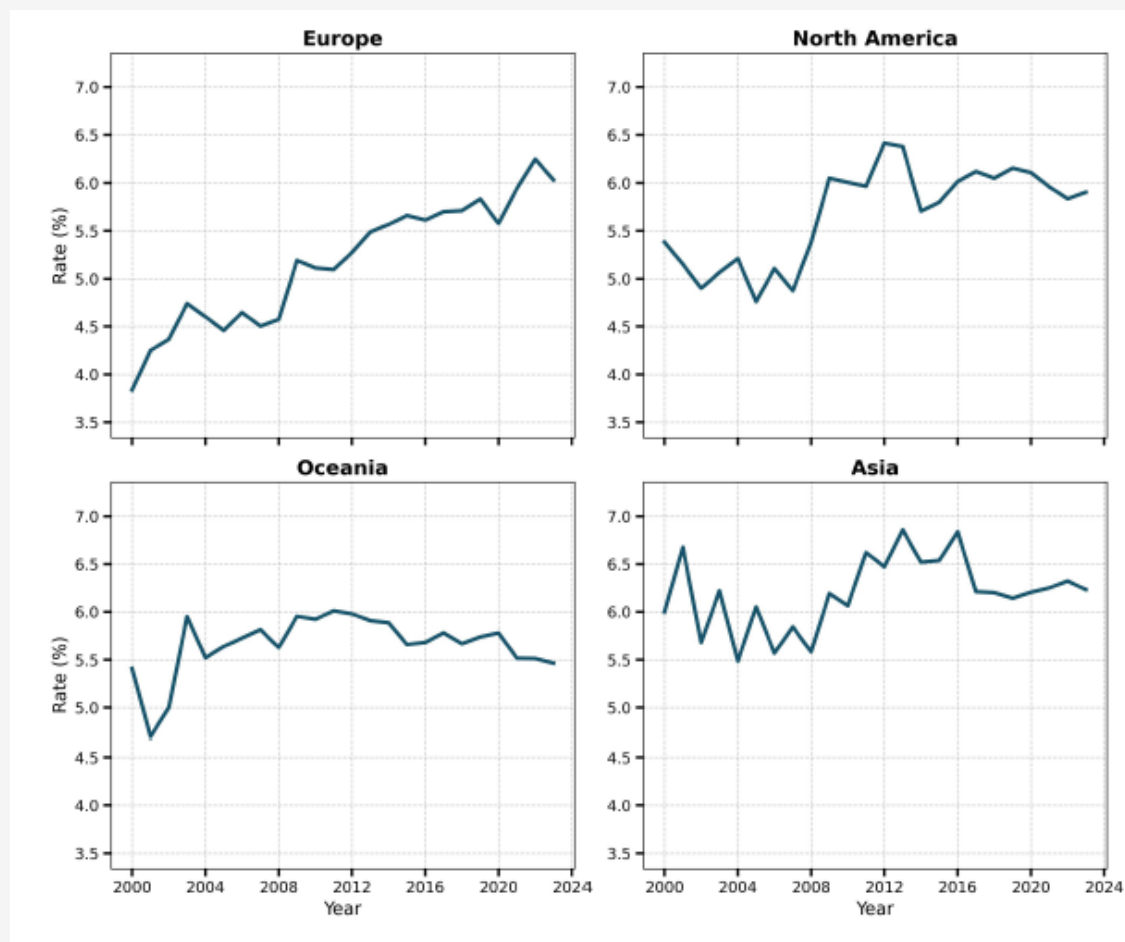
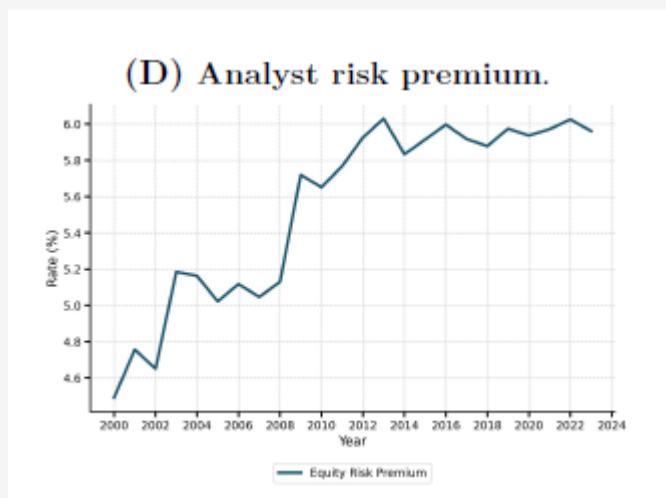
Panel B: SML regression:

	1-year realized return _{i,j,t}					
	(1) Analyst beta	(2) 24-month	(3) 36-month	(4) 48-month	(5) 60-month	(6) 72-month
Beta _{i,j,t}	7.89*** (1.57)	2.65*** (0.72)	2.07** (0.81)	4.29*** (0.83)	3.05*** (0.87)	2.43*** (0.76)
Constant	0.69 (1.64)	7.12*** (0.68)	7.52*** (0.75)	5.54*** (0.76)	6.53*** (0.79)	6.78*** (0.73)
Observations	15,143	13,749	13,212	12,650	12,083	11,584
F Statistics	25.12	13.75	6.59	26.79	12.32	10.30
R ²	0.00	0.00	0.00	0.00	0.00	0.00

- These patterns show that analysts' betas contain additional information missed in standard CAPM estimation

Equity Risk Premium – Descriptive

- The equity risk premium has increased over time, creating a doubt on whether analysts use a fixed value as their estimate
- Even though it has increased, analysts use different prices of systematic risk across regions over time
- The measure displays volatility in most regions suggesting that subjective risk premia are relatively flat



Discount Rates – Growth Expectations

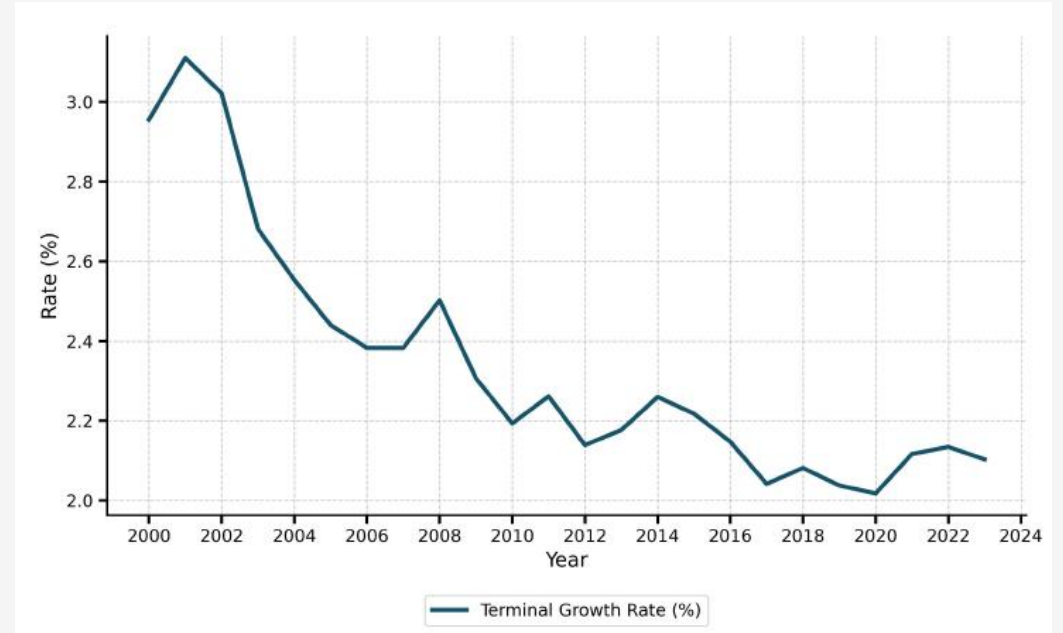
- Check whether discount rates offset optimistic terminal growth rate

Dependent variable:	Discount rate _{i,j,t} (%)	
	(1)	(2)
TGR _{i,j,t} (%)	0.27*** (0.01)	0.03** (0.01)
Analyst*Firm FE	No	Yes
Year FE	No	Yes
Observations	48,927	37,662
F Statistics	487.53	6.21
R ²	0.03	0.76

- When it comes to within-analyst (2), even though the TGR is significant, its coefficient is of negligible economic magnitude
- **Analysts do not adjust their discount rates to balance growth expectations**

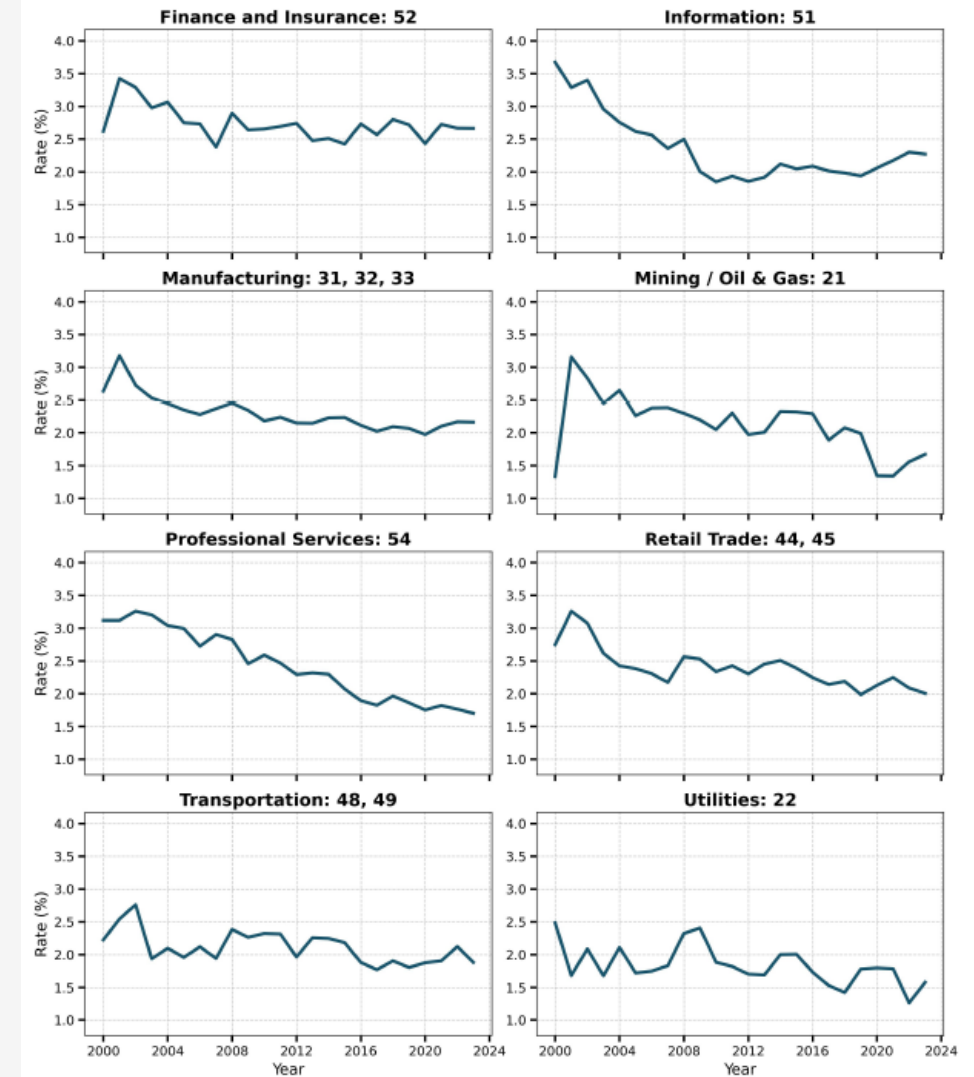
Terminal Growth Rate – Descriptive

- The average growth rate has steadily declined over the years



Terminal Growth Rate – Descriptive

- But the decrease has happened differently across the different industries
- Commodities and retail have even recovered from the decrease



Terminal Growth Rate – Regression

Terminal growth rates and Macroeconomic Variables	Terminal growth rate _{c,t} (%)				
	(1)	(2)	(3)	(4)	(5)
	Current	10-year hist. avg.	SPF 10-year forecast	Current	10-year hist. avg.
	US Only			Full Sample	
Inflation _{c,t} (%)	0.00 (0.03)	-0.15 (0.18)	0.60 (0.49)	0.00 (0.01)	0.01 (0.04)
Real GDP growth _{c,t} (%)	0.01 (0.03)	0.35*** (0.09)	0.63*** (0.17)	0.01*** (0.00)	0.09*** (0.03)
10-year treasury yield _{c,t} (%)	0.35*** (0.06)	0.25*** (0.08)	0.25*** (0.07)	0.03** (0.01)	0.05* (0.02)
Country FE	No	No	No	Yes	Yes
Observations	23	23	23	605	605
F Statistics	9.88	68.12	47.26	5.45	4.34
R ²	0.74	0.92	0.83	0.64	0.66
Within R ²	0.74	0.92	0.83	0.03	0.07
R ² Shapley Decomposition					
Inflation _{c,t} (%)	0.29 %	17.05 %	23.99 %	4.67 %	13.76 %
Real GDP growth _{c,t} (%)	1.49 %	40.92 %	39.73 %	45.09 %	41.72 %
10-year treasury yield _{c,t} (%)	98.23 %	42.03 %	36.28 %	50.24 %	44.51 %

- When it comes to current levels, 10-year historical average or 10-year forecast, the mean shows more explanatory power due to its bigger R²
- Analysts anchor their long-term expectations on historical GDP and 10-year treasury yield realizations, which aligns with the risk-free and discount rates components

Discount Rates – Key Macroeconomic Values Regression

- Key macroeconomic values: current inflation rate and 10-year inflation expectations

Panel B: Inflation & Treasury yield	Discount rate _{c,t} (%)			
	(1)	(2)	(3)	(4)
		US Only		
Inflation rate _{c,t} (%)	0.02 (0.02)	-0.22*** (0.04)		
10-Year inflation expectations _{c,t} (%)		3.90*** (0.74)		
Analyst risk-free rate _{c,t} (%)			0.29*** (0.04)	
10-year treasury yield _{c,t} (%)				0.20*** (0.04)
Country FE	Yes	No	Yes	Yes
Observations	1,195	23	871	871
F Statistics	1.06	18.98	69.27	24.56
Within R ²	0.01	0.60	0.25	0.24

- By (1) and (2), current inflation rates have limited explanatory power on discount rates
- (3) and (4) show that risk-free and 10-year Treasury yield benchmark have a similar coefficient, suggesting that changes in monetary policies are readily reflected in the analysts' discount rate

Main Conclusions

- **Discount Rate as a Key Driver:** The discount rate is a primary determinant in explaining variations in expected firm valuations, often as impactful as growth expectations
- **Components and Fluctuations:** The primary drivers of discount rate variations are the risk-free rate and equity beta. Both components contain internal factors — such as long-term economic trends and systematic risk — that align with the study's broader conclusions on how discount rates respond to economic conditions
- **Alignment with Market Requirements:** Analysts' discount rates closely mirror the real-world return expectations, suggesting they capture inherent market requirements accurately
- **Independence from Growth Expectations:** Analysts do not systematically adjust discount rates to offset optimistic growth expectations
- **Influence of Economic Conditions:** Discount rates are affected by long-term economic variables such as inflation expectations and GDP growth but exhibit little responsiveness to short-term inflation fluctuations.

Obrigado

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